

- 1** In an arithmetic series, the 6th term is 39
In the same arithmetic series, the 19th term is 7.8

Work out the sum of the first 25 terms of the arithmetic series.

(Total for Question 1 is 4 marks)

2 Here are the first five terms of an arithmetic sequence.

8 15 22 29 36

Work out the sum of all the terms from the 50th term to the 100th term inclusive.

(Total for Question 2 is 4 marks)

- 3** The first term of an arithmetic series S is -6
The sum of the first 30 terms of S is 2865
Find the 9th term of S .

.....
(Total for Question 3 is 4 marks)

4 Mario is going to save \$50 in the year 2021

He is going to continue to save, up to and including the year 2070, by increasing the amount he saves each year by \$ k

Mario will save a total of \$33 125 from 2021 to 2070

Work out the value of k .

$k = \dots\dots\dots$

(Total for Question 4 is 3 marks)

5 Here are the first 4 terms of an arithmetic sequence.

85 79 73 67

Find an expression, in terms of n , for the n th term of the sequence.

.....
(Total for Question 5 is 2 marks)

6 The sum of the first N terms of an arithmetic series, S , is 292

The 2nd term of S is 8.5

The 5th term of S is 13

Find the value of N .

Show clear algebraic working.

$N =$

(Total for Question 6 is 5 marks)

- 7 The n th term of an arithmetic series is u_n where $u_n > 0$ for all n
The sum to n terms of the series is S_n

Given that $u_4 = 6$ and that $S_{11} = (u_6)^2 + 18$

find the value of u_{20}

.....

(Total for Question 7 is 6 marks)

8 An arithmetic series has first term a and common difference d .

The sum of the first $2n$ terms of the series is four times the sum of the first n terms of the series.

Find an expression for a in terms of d .
Show your working clearly.

$$a = \dots\dots\dots$$

(Total for Question 8 is 4 marks)

These two types of shelves are arranged into shelving units that form a sequence of patterns.

The diagram illustrates three different arrangements of rectangular blocks labeled R and S. Arrangement 1 shows three blocks in a row: R, S, and R. Arrangement 2 shows five blocks in a row: R, S, R, S, and R. Below this arrangement, two double-headed arrows indicate dimensions: 2.4m between the first and second blocks, and 3.5m between the third and fourth blocks. Arrangement 3 shows seven blocks in a row: R, S, R, S, R, S, and R.

(a) Work out the total width of a shelving unit that has 6 type **R** shelves.

(Total for Question 9 is 4 marks)

- 10** The sum of the first 10 terms of an arithmetic series is 4 times the sum of the first 5 terms of the same series.

The 8th term of this series is 45

Find the first term of this series.

Show clear algebraic working.

(Total for Question 10 is 5 marks)

11 Here are the first five terms of an arithmetic sequence.

1 5 9 13 17

(a) Find an expression, in terms of n , for the n th term of this sequence.

.....
(2)

The n th term of another arithmetic sequence is $3n + 5$

(b) Find an expression, in terms of m , for the $(2m)$ th term of this sequence.

.....
(1)

(Total for Question 11 is 3 marks)

12 A polygon has n sides, where $n > 5$

When arranged in order of size, starting with the largest number, the sizes of the interior angles of the polygon, in degrees, are the terms of an arithmetic sequence.

Here are the first five terms of this sequence.

177 175 173 171 169

Find the value of n

Show clear algebraic working.

$$n = \dots\dots\dots$$

(Total for Question 12 is 6 marks)

13 An arithmetic series has first term 1 and common difference 4

Find the sum of all terms of the series from the 41st term to the 100th term inclusive.

(Total for Question 13 is 4 marks)

- 14** An arithmetic series has first term a and common difference d , where d is a prime number.

The sum of the first n terms of the series is S_n and

$$S_m = 39$$

$$S_{2m} = 320$$

Find the value of d and the value of m

Show clear algebraic working.

$$d = \dots\dots\dots$$

$$m = \dots\dots\dots$$

(Total for Question 14 is 5 marks)

- 15** An arithmetic sequence has first term 8 and common difference 11
The sequence has k terms, where $k > 21$

The sum of the last 20 terms of the sequence is 10 170

Find the value of k

Show clear algebraic working.

$k = \dots\dots\dots$

(Total for Question 15 is 5 marks)

- 16** The first term of an arithmetic series is $(2t + 1)$ where $t > 0$
The n th term of this arithmetic series is $(14t - 5)$

The common difference of the series is 3

The sum of the first n terms of the series can be written as $p(qt - 1)^r$ where p , q and r are integers.

Find the value of p , the value of q and the value of r
Show clear algebraic working.

$$p = \dots\dots\dots q = \dots\dots\dots r = \dots\dots\dots$$

(Total for Question 16 is 4 marks)

17 Here are the first four terms of an arithmetic sequence.

38 31 24 17

Find an expression, in terms of n , for the n th term of the sequence.

(Total for Question 17 is 2 marks)

18 Here are the first three terms of an arithmetic sequence.

$$8p \qquad 7p - 3 \qquad 4p + 2$$

The sum of the first n terms of the sequence is -1914

Work out the value of n

Show your working clearly.

$$n = \dots\dots\dots$$

(Total for Question 18 is 5 marks)

19 The sum of the first 80 terms of an arithmetic series, S , is 470

The 75th term of S is 14.5

The sum of the first X terms of S is 171

Work out the value of X

Show your working clearly.

$$X = \dots\dots\dots$$

(Total for Question 19 is 6 marks)